

# 1 Sebastian's math test

The default math mode font is *Math Italic*. This should not be confused with ordinary *Text Italic* – notice the different spacing! `\mathbf` produces bold roman letters: **abcABC**. If you wish to embolden complete formulas, use the `\boldmath` command *before* going into math mode. This changes the default math fonts to bold.

```
normal       $x = 2\pi \Rightarrow x \simeq 6.28$ 
mathbf       $\mathbf{x} = 2\pi \Rightarrow \mathbf{x} \simeq 6.28$ 
boldmath     $\mathbf{x} = 2\pi \Rightarrow \mathbf{x} \simeq \mathbf{6.28}$ 
```

Greek is available in upper and lower case:  $\alpha, \beta \dots \Omega$ , and there are special symbols such as  $\hbar$  (compare to  $h$ ). Digits in formulas 1, 2, 3 ... may differ from those in text: 4, 5, 6 ...

There is Sans Serif alphabet abcdeABCD selected by `\mathsf` and Type-writer math abcdeABCD selected by `\mathtt`.

There is a calligraphic alphabet `\mathcal` for upper case letters  $\mathcal{A}\mathcal{B}\mathcal{C}\mathcal{D}\mathcal{E} \dots$ , and there are letters for number sets:  $\mathbb{A} \dots \mathbb{Z}$ , which are produced using `\mathbb`. There are Fraktur letters abcde $\mathfrak{A}\mathfrak{B}\mathfrak{C}\mathfrak{D}\mathfrak{E}$  produced using `\mathfrak`

$$\sigma(t) = \frac{1}{\sqrt{2\pi}} \int_0^t e^{-x^2/2} dx \quad (1)$$

$$\prod_{j \geq 0} \left( \sum_{k \geq 0} a_{jk} z^k \right) = \sum_{k \geq 0} z^n \left( \sum_{\substack{k_0, k_1, \dots \geq 0 \\ k_0 + k_1 + \dots = n}} a_0 k_0 a_1 k_1 \dots \right) \quad (2)$$

$$\pi(n) = \sum_{m=2}^n \left\lfloor \left( \sum_{k=1}^{m-1} \lfloor (m/k)/\lceil m/k \rceil \rfloor \right)^{-1} \right\rfloor \quad (3)$$

$$\underbrace{\{a, \dots, a\}}_{k+l \text{ elements}}, \underbrace{\{b, \dots, b\}}_{l \text{ } b's} \quad (4)$$

$$\begin{aligned} W^+ &\nearrow \mu^+ + \nu_\mu \\ &\rightarrow \pi^+ + \pi^0 \\ &\rightarrow \kappa^+ + \pi^0 \\ &\searrow e^+ + \nu_e \end{aligned}$$

$$\pm \frac{\left| \begin{array}{ccc} x_1 - x_2 & y_1 - y_2 & z_1 - z_2 \\ l_1 & m_1 & n_1 \\ l_2 & m_2 & n_2 \end{array} \right|}{\sqrt{\left| \begin{array}{cc} l_1 & m_1 \\ l_2 & m_2 \end{array} \right|^2 + \left| \begin{array}{cc} m_1 & n_1 \\ n_1 & l_1 \end{array} \right|^2 + \left| \begin{array}{cc} m_2 & n_2 \\ n_2 & l_2 \end{array} \right|^2}}$$

## 2 Math Tests

Math test are taken from[1].

### 2.1 Math Alphabets

Math Italic (\mathnormal)

A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z,  
a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z, i, J,  
A, B,  $\Gamma$ ,  $\Delta$ , E, Z, H,  $\Theta$ , I, K, A, M, N,  $\Xi$ , O,  $\Pi$ , P,  $\Sigma$ , T,  $\Upsilon$ ,  $\Phi$ , X,  $\Psi$ ,  $\Omega$ ,  
 $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ ,  $\epsilon$ ,  $\zeta$ ,  $\eta$ ,  $\theta$ ,  $\iota$ ,  $\kappa$ ,  $\lambda$ ,  $\mu$ ,  $\nu$ ,  $\xi$ , o,  $\pi$ ,  $\rho$ ,  $\sigma$ ,  $\tau$ ,  $v$ ,  $\phi$ ,  $\chi$ ,  $\psi$ ,  $\omega$ ,  $\varepsilon$ ,  $\vartheta$ ,  $\varpi$ ,  $\varrho$ ,  $\varsigma$ ,  $\varphi$ ,  $\ell$ ,  $\wp$ ,

Math Roman (\mathrm)

0, 1, 2, 3, 4, 5, 6, 7, 8, 9,  
A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z,  
a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z, i, J,  
A, B,  $\Gamma$ ,  $\Delta$ , E, Z, H,  $\Theta$ , I, K,  $\Lambda$ , M, N,  $\Xi$ , O,  $\Pi$ , P,  $\Sigma$ , T,  $\Upsilon$ ,  $\Phi$ , X,  $\Psi$ ,  $\Omega$ ,  
 $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ ,  $\epsilon$ ,  $\zeta$ ,  $\eta$ ,  $\theta$ ,  $\iota$ ,  $\kappa$ ,  $\lambda$ ,  $\mu$ ,  $\nu$ ,  $\xi$ , o,  $\pi$ ,  $\rho$ ,  $\sigma$ ,  $\tau$ ,  $v$ ,  $\phi$ ,  $\chi$ ,  $\psi$ ,  $\omega$ ,  $\varepsilon$ ,  $\vartheta$ ,  $\varpi$ ,  $\varrho$ ,  $\varsigma$ ,  $\varphi$ ,  $\ell$ ,  $\wp$ ,

Math Bold (\mathbf)

**0, 1, 2, 3, 4, 5, 6, 7, 8, 9,**  
**A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z,**  
**a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z, i, J,**

Math Sans Serif (\mathsf)

0, 1, 2, 3, 4, 5, 6, 7, 8, 9,  
A, B, C, D, E, F, G, H, I, J, K, L, M, N, O, P, Q, R, S, T, U, V, W, X, Y, Z,  
a, b, c, d, e, f, g, h, i, j, k, l, m, n, o, p, q, r, s, t, u, v, w, x, y, z, i, J,

Caligraphic (\mathcal)

$\mathcal{A}, \mathcal{B}, \mathcal{C}, \mathcal{D}, \mathcal{E}, \mathcal{F}, \mathcal{G}, \mathcal{H}, \mathcal{I}, \mathcal{J}, \mathcal{K}, \mathcal{L}, \mathcal{M}, \mathcal{N}, \mathcal{O}, \mathcal{P}, \mathcal{Q}, \mathcal{R}, \mathcal{S}, \mathcal{T}, \mathcal{U}, \mathcal{V}, \mathcal{W}, \mathcal{X}, \mathcal{Y}, \mathcal{Z}$ ,

Fraktur (\mathfrak)

$\mathfrak{A}, \mathfrak{B}, \mathfrak{C}, \mathfrak{D}, \mathfrak{E}, \mathfrak{F}, \mathfrak{G}, \mathfrak{H}, \mathfrak{I}, \mathfrak{J}, \mathfrak{K}, \mathfrak{L}, \mathfrak{M}, \mathfrak{N}, \mathfrak{O}, \mathfrak{P}, \mathfrak{Q}, \mathfrak{R}, \mathfrak{S}, \mathfrak{T}, \mathfrak{U}, \mathfrak{V}, \mathfrak{W}, \mathfrak{X}, \mathfrak{Y}, \mathfrak{Z}$ ,  
 $\mathfrak{a}, \mathfrak{b}, \mathfrak{c}, \mathfrak{d}, \mathfrak{e}, \mathfrak{f}, \mathfrak{g}, \mathfrak{h}, \mathfrak{i}, \mathfrak{j}, \mathfrak{k}, \mathfrak{l}, \mathfrak{m}, \mathfrak{n}, \mathfrak{o}, \mathfrak{p}, \mathfrak{q}, \mathfrak{r}, \mathfrak{s}, \mathfrak{t}, \mathfrak{u}, \mathfrak{v}, \mathfrak{w}, \mathfrak{x}, \mathfrak{y}, \mathfrak{z}, \mathfrak{i}, \mathfrak{J}$ ,

Blackboard Bold (\mathbb)

$\mathbb{A}, \mathbb{B}, \mathbb{C}, \mathbb{D}, \mathbb{E}, \mathbb{F}, \mathbb{G}, \mathbb{H}, \mathbb{I}, \mathbb{J}, \mathbb{K}, \mathbb{L}, \mathbb{M}, \mathbb{N}, \mathbb{O}, \mathbb{P}, \mathbb{Q}, \mathbb{R}, \mathbb{S}, \mathbb{T}, \mathbb{U}, \mathbb{V}, \mathbb{W}, \mathbb{X}, \mathbb{Y}, \mathbb{Z}$ ,

## 2.2 Character Sidebearings

$|A| + |B| + |C| + |D| + |E| + |F| + |G| + |H| + |I| + |J| + |K| + |L| + |M| +$   
 $|N| + |O| + |P| + |Q| + |R| + |S| + |T| + |U| + |V| + |W| + |X| + |Y| + |Z| +$   
 $|a| + |b| + |c| + |d| + |e| + |f| + |g| + |h| + |i| + |j| + |k| + |l| + |m| +$   
 $|n| + |o| + |p| + |q| + |r| + |s| + |t| + |u| + |v| + |w| + |x| + |y| + |z| + |i| + |j| +$   
 $|A| + |B| + |\Gamma| + |\Delta| + |E| + |Z| + |H| + |\Theta| + |I| + |K| + |\Lambda| + |M| +$   
 $|N| + |\Xi| + |O| + |\Pi| + |P| + |\Sigma| + |T| + |\Upsilon| + |\Phi| + |X| + |\Psi| + |\Omega| +$   
 $|\alpha| + |\beta| + |\gamma| + |\delta| + |\epsilon| + |\zeta| + |\eta| + |\theta| + |\iota| + |\kappa| + |\lambda| + |\mu| +$   
 $|\nu| + |\xi| + |\sigma| + |\pi| + |\rho| + |\sigma| + |\tau| + |\nu| + |\phi| + |\chi| + |\psi| + |\omega| +$   
 $|\varepsilon| + |\vartheta| + |\varpi| + |\varrho| + |\varsigma| + |\varphi| + |\ell| + |\wp| +$

$|A| + |B| + |C| + |D| + |E| + |F| + |G| + |H| + |I| + |J| + |K| + |L| + |M| +$   
 $|N| + |O| + |P| + |Q| + |R| + |S| + |T| + |U| + |V| + |W| + |X| + |Y| + |Z| +$   
 $|a| + |b| + |c| + |d| + |e| + |f| + |g| + |h| + |i| + |j| + |k| + |l| + |m| +$   
 $|n| + |o| + |p| + |q| + |r| + |s| + |t| + |u| + |v| + |w| + |x| + |y| + |z| + |i| + |j| +$   
 $|A| + |B| + |\Gamma| + |\Delta| + |E| + |Z| + |H| + |\Theta| + |I| + |K| + |\Lambda| + |M| +$   
 $|N| + |\Xi| + |O| + |\Pi| + |P| + |\Sigma| + |T| + |\Upsilon| + |\Phi| + |X| + |\Psi| + |\Omega| +$

$|\mathcal{A}| + |\mathcal{B}| + |\mathcal{C}| + |\mathcal{D}| + |\mathcal{E}| + |\mathcal{F}| + |\mathcal{G}| + |\mathcal{H}| + |\mathcal{I}| + |\mathcal{J}| + |\mathcal{K}| + |\mathcal{L}| + |\mathcal{M}| +$   
 $|\mathcal{N}| + |\mathcal{O}| + |\mathcal{P}| + |\mathcal{Q}| + |\mathcal{R}| + |\mathcal{S}| + |\mathcal{T}| + |\mathcal{U}| + |\mathcal{V}| + |\mathcal{W}| + |\mathcal{X}| + |\mathcal{Y}| + |\mathcal{Z}| +$

## 2.3 Superscript positioning

$$\begin{aligned}
& A^2 + B^2 + C^2 + D^2 + E^2 + F^2 + G^2 + H^2 + I^2 + J^2 + K^2 + L^2 + M^2 + \\
& N^2 + O^2 + P^2 + Q^2 + R^2 + S^2 + T^2 + U^2 + V^2 + W^2 + X^2 + Y^2 + Z^2 + \\
& a^2 + b^2 + c^2 + d^2 + e^2 + f^2 + g^2 + h^2 + i^2 + j^2 + k^2 + l^2 + m^2 + \\
& n^2 + o^2 + p^2 + q^2 + r^2 + s^2 + t^2 + u^2 + v^2 + w^2 + x^2 + y^2 + z^2 + i^2 + j^2 + \\
& A^2 + B^2 + \Gamma^2 + \Delta^2 + E^2 + Z^2 + H^2 + \Theta^2 + I^2 + K^2 + \Lambda^2 + M^2 + \\
& N^2 + \Xi^2 + O^2 + \Pi^2 + P^2 + \Sigma^2 + T^2 + \Upsilon^2 + \Phi^2 + X^2 + \Psi^2 + \Omega^2 + \\
& \alpha^2 + \beta^2 + \gamma^2 + \delta^2 + \epsilon^2 + \zeta^2 + \eta^2 + \theta^2 + i^2 + \kappa^2 + \lambda^2 + \mu^2 + \\
& v^2 + \xi^2 + o^2 + \pi^2 + \rho^2 + \sigma^2 + \tau^2 + v^2 + \phi^2 + \chi^2 + \psi^2 + \omega^2 + \\
& \varepsilon^2 + \vartheta^2 + \varpi^2 + \varrho^2 + \varsigma^2 + \varphi^2 + \ell^2 + \wp^2 +
\end{aligned}$$

$$\begin{aligned}
& A^2 + B^2 + C^2 + D^2 + E^2 + F^2 + G^2 + H^2 + I^2 + J^2 + K^2 + L^2 + M^2 + \\
& N^2 + O^2 + P^2 + Q^2 + R^2 + S^2 + T^2 + U^2 + V^2 + W^2 + X^2 + Y^2 + Z^2 + \\
& a^2 + b^2 + c^2 + d^2 + e^2 + f^2 + g^2 + h^2 + i^2 + j^2 + k^2 + l^2 + m^2 + \\
& n^2 + o^2 + p^2 + q^2 + r^2 + s^2 + t^2 + u^2 + v^2 + w^2 + x^2 + y^2 + z^2 + i^2 + j^2 + \\
& A^2 + B^2 + \Gamma^2 + \Delta^2 + E^2 + Z^2 + H^2 + \Theta^2 + I^2 + K^2 + \Lambda^2 + M^2 + \\
& N^2 + \Xi^2 + O^2 + \Pi^2 + P^2 + \Sigma^2 + T^2 + \Upsilon^2 + \Phi^2 + X^2 + \Psi^2 + \Omega^2 +
\end{aligned}$$

$$\begin{aligned}
& \mathcal{A}^2 + \mathcal{B}^2 + \mathcal{C}^2 + \mathcal{D}^2 + \mathcal{E}^2 + \mathcal{F}^2 + \mathcal{G}^2 + \mathcal{H}^2 + \mathcal{I}^2 + \mathcal{J}^2 + \mathcal{K}^2 + \mathcal{L}^2 + \mathcal{M}^2 + \\
& \mathcal{N}^2 + \mathcal{O}^2 + \mathcal{P}^2 + \mathcal{Q}^2 + \mathcal{R}^2 + \mathcal{S}^2 + \mathcal{T}^2 + \mathcal{U}^2 + \mathcal{V}^2 + \mathcal{W}^2 + \mathcal{X}^2 + \mathcal{Y}^2 + \mathcal{Z}^2 +
\end{aligned}$$

## 2.4 Subscript positioning

$A_i + B_i + C_i + D_i + E_i + F_i + G_i + H_i + I_i + J_i + K_i + L_i + M_i +$   
 $N_i + O_i + P_i + Q_i + R_i + S_i + T_i + U_i + V_i + W_i + X_i + Y_i + Z_i +$   
 $a_i + b_i + c_i + d_i + e_i + f_i + g_i + h_i + i_i + j_i + k_i + l_i + m_i +$   
 $n_i + o_i + p_i + q_i + r_i + s_i + t_i + u_i + v_i + w_i + x_i + y_i + z_i + i_i + j_i +$   
 $A_i + B_i + \Gamma_i + \Delta_i + E_i + Z_i + H_i + \Theta_i + I_i + K_i + \Lambda_i + M_i +$   
 $N_i + \Xi_i + O_i + \Pi_i + P_i + \Sigma_i + T_i + \Upsilon_i + \Phi_i + X_i + \Psi_i + \Omega_i +$   
 $\alpha_i + \beta_i + \gamma_i + \delta_i + \epsilon_i + \zeta_i + \eta_i + \theta_i + \iota_i + \kappa_i + \lambda_i + \mu_i +$   
 $\nu_i + \xi_i + o_i + \pi_i + \rho_i + \sigma_i + \tau_i + v_i + \phi_i + \chi_i + \psi_i + \omega_i +$   
 $\varepsilon_i + \vartheta_i + \varpi_i + \varrho_i + \varsigma_i + \varphi_i + \ell_i + \wp_i +$

$A_i + B_i + C_i + D_i + E_i + F_i + G_i + H_i + I_i + J_i + K_i + L_i + M_i +$   
 $N_i + O_i + P_i + Q_i + R_i + S_i + T_i + U_i + V_i + W_i + X_i + Y_i + Z_i +$   
 $a_i + b_i + c_i + d_i + e_i + f_i + g_i + h_i + i_i + j_i + k_i + l_i + m_i +$   
 $n_i + o_i + p_i + q_i + r_i + s_i + t_i + u_i + v_i + w_i + x_i + y_i + z_i + i_i + j_i +$   
 $A_i + B_i + \Gamma_i + \Delta_i + E_i + Z_i + H_i + \Theta_i + I_i + K_i + \Lambda_i + M_i +$   
 $N_i + \Xi_i + O_i + \Pi_i + P_i + \Sigma_i + T_i + \Upsilon_i + \Phi_i + X_i + \Psi_i + \Omega_i +$

$\mathcal{A}_i + \mathcal{B}_i + \mathcal{C}_i + \mathcal{D}_i + \mathcal{E}_i + \mathcal{F}_i + \mathcal{G}_i + \mathcal{H}_i + \mathcal{I}_i + \mathcal{J}_i + \mathcal{K}_i + \mathcal{L}_i + \mathcal{M}_i +$   
 $\mathcal{N}_i + \mathcal{O}_i + \mathcal{P}_i + \mathcal{Q}_i + \mathcal{R}_i + \mathcal{S}_i + \mathcal{T}_i + \mathcal{U}_i + \mathcal{V}_i + \mathcal{W}_i + \mathcal{X}_i + \mathcal{Y}_i + \mathcal{Z}_i +$

## 2.5 Accent positioning

$\hat{A} + \hat{B} + \hat{C} + \hat{D} + \hat{E} + \hat{F} + \hat{G} + \hat{H} + \hat{I} + \hat{J} + \hat{K} + \hat{L} + \hat{M} +$   
 $\hat{N} + \hat{O} + \hat{P} + \hat{Q} + \hat{R} + \hat{S} + \hat{T} + \hat{U} + \hat{V} + \hat{W} + \hat{X} + \hat{Y} + \hat{Z} +$   
 $\hat{a} + \hat{b} + \hat{c} + \hat{d} + \hat{e} + \hat{f} + \hat{g} + \hat{h} + \hat{i} + \hat{j} + \hat{k} + \hat{l} + \hat{m} +$   
 $\hat{n} + \hat{o} + \hat{p} + \hat{q} + \hat{r} + \hat{s} + \hat{t} + \hat{u} + \hat{v} + \hat{w} + \hat{x} + \hat{y} + \hat{z} + \hat{i} + \hat{j} +$   
 $\hat{A} + \hat{B} + \hat{\Gamma} + \hat{\Delta} + \hat{E} + \hat{Z} + \hat{H} + \hat{\Theta} + \hat{I} + \hat{K} + \hat{\Lambda} + \hat{M} +$   
 $\hat{N} + \hat{\Xi} + \hat{O} + \hat{\Pi} + \hat{P} + \hat{\Sigma} + \hat{T} + \hat{\Upsilon} + \hat{\Phi} + \hat{X} + \hat{\Psi} + \hat{\Omega} +$   
 $\hat{\alpha} + \hat{\beta} + \hat{\gamma} + \hat{\delta} + \hat{\epsilon} + \hat{\zeta} + \hat{\eta} + \hat{\theta} + \hat{i} + \hat{k} + \hat{\lambda} + \hat{\mu} +$   
 $\hat{v} + \hat{\xi} + \hat{o} + \hat{\pi} + \hat{p} + \hat{\sigma} + \hat{\tau} + \hat{v} + \hat{\phi} + \hat{\chi} + \hat{\psi} + \hat{\omega} +$   
 $\hat{\varepsilon} + \hat{\vartheta} + \hat{\varpi} + \hat{\varrho} + \hat{\varsigma} + \hat{\varphi} + \hat{\ell} + \hat{\wp} +$

$\hat{A} + \hat{B} + \hat{C} + \hat{D} + \hat{E} + \hat{F} + \hat{G} + \hat{H} + \hat{I} + \hat{J} + \hat{K} + \hat{L} + \hat{M} +$   
 $\hat{N} + \hat{O} + \hat{P} + \hat{Q} + \hat{R} + \hat{S} + \hat{T} + \hat{U} + \hat{V} + \hat{W} + \hat{X} + \hat{Y} + \hat{Z} +$   
 $\hat{a} + \hat{b} + \hat{c} + \hat{d} + \hat{e} + \hat{f} + \hat{g} + \hat{h} + \hat{i} + \hat{j} + \hat{k} + \hat{l} + \hat{m} +$   
 $\hat{n} + \hat{o} + \hat{p} + \hat{q} + \hat{r} + \hat{s} + \hat{t} + \hat{u} + \hat{v} + \hat{w} + \hat{x} + \hat{y} + \hat{z} + \hat{i} + \hat{j} +$

$\hat{A} + \hat{B} + \hat{C} + \hat{D} + \hat{E} + \hat{F} + \hat{G} + \hat{H} + \hat{I} + \hat{J} + \hat{K} + \hat{L} + \hat{M} +$   
 $\hat{N} + \hat{O} + \hat{P} + \hat{Q} + \hat{R} + \hat{S} + \hat{T} + \hat{U} + \hat{V} + \hat{W} + \hat{X} + \hat{Y} + \hat{Z} +$

## 2.6 Differentials

$$\begin{aligned}
& dA + dB + dC + dD + dE + dF + dG + dH + dI + dJ + dK + dL + dM + \\
& dN + dO + dP + dQ + dR + dS + dT + dU + dV + dW + dX + dY + dZ + \\
& da + db + dc + dd + de + df + dg + dh + di + dj + dk + dl + dm + \\
& dn + do + dp + dq + dr + ds + dt + du + dv + dw + dx + dy + dz + di + dj + \\
& dA + dB + d\Gamma + d\Delta + dE + dZ + dH + d\Theta + dI + dK + d\Lambda + dM + \\
& dN + d\Xi + dO + d\Pi + dP + d\Sigma + dT + d\Upsilon + d\Phi + dX + d\Psi + d\Omega + \\
& d\alpha + d\beta + d\gamma + d\delta + d\epsilon + d\zeta + d\eta + d\theta + di + dk + d\kappa + d\lambda + d\mu + \\
& dv + d\xi + do + d\pi + d\rho + d\sigma + d\tau + dv + d\phi + d\chi + d\psi + d\omega + \\
& d\varepsilon + d\vartheta + d\varpi + d\varrho + d\varsigma + d\varphi + d\ell + d\wp + \\
& dA + dB + d\Gamma + d\Delta + dE + dZ + dH + d\Theta + dI + dK + d\Lambda + dM + \\
& dN + d\Xi + dO + d\Pi + dP + d\Sigma + dT + d\Upsilon + d\Phi + dX + d\Psi + d\Omega + \\
\\
& dA + dB + dC + dD + dE + dF + dG + dH + dI + dJ + dK + dL + dM + \\
& dN + dO + dP + dQ + dR + dS + dT + dU + dV + dW + dX + dY + dZ + \\
& da + db + dc + dd + de + df + dg + dh + di + dj + dk + dl + dm + \\
& dn + do + dp + dq + dr + ds + dt + du + dv + dw + dx + dy + dz + di + dj + \\
& dA + dB + d\Gamma + d\Delta + dE + dZ + dH + d\Theta + dI + dK + d\Lambda + dM + \\
& dN + d\Xi + dO + d\Pi + dP + d\Sigma + dT + d\Upsilon + d\Phi + dX + d\Psi + d\Omega + \\
& d\alpha + d\beta + d\gamma + d\delta + d\epsilon + d\zeta + d\eta + d\theta + di + dk + d\kappa + d\lambda + d\mu + \\
& dv + d\xi + do + d\pi + d\rho + d\sigma + d\tau + dv + d\phi + d\chi + d\psi + d\omega + \\
& d\varepsilon + d\vartheta + d\varpi + d\varrho + d\varsigma + d\varphi + d\ell + d\wp + \\
& dA + dB + d\Gamma + d\Delta + dE + dZ + dH + d\Theta + dI + dK + d\Lambda + dM + \\
& dN + d\Xi + dO + d\Pi + dP + d\Sigma + dT + d\Upsilon + d\Phi + dX + d\Psi + d\Omega + \\
\\
& \partial A + \partial B + \partial C + \partial D + \partial E + \partial F + \partial G + \partial H + \partial I + \partial J + \partial K + \partial L + \partial M + \\
& \partial N + \partial O + \partial P + \partial Q + \partial R + \partial S + \partial T + \partial U + \partial V + \partial W + \partial X + \partial Y + \partial Z + \\
& \partial a + \partial b + \partial c + \partial d + \partial e + \partial f + \partial g + \partial h + \partial i + \partial j + \partial k + \partial l + \partial m + \\
& \partial n + \partial o + \partial p + \partial q + \partial r + \partial s + \partial t + \partial u + \partial v + \partial w + \partial x + \partial y + \partial z + \partial i + \partial j + \\
& \partial A + \partial B + \partial \Gamma + \partial \Delta + \partial E + \partial Z + \partial H + \partial \Theta + \partial I + \partial K + \partial \Lambda + \partial M + \\
& \partial N + \partial \Xi + \partial O + \partial \Pi + \partial P + \partial \Sigma + \partial T + \partial \Upsilon + \partial \Phi + \partial X + \partial \Psi + \partial \Omega + \\
& \partial \alpha + \partial \beta + \partial \gamma + \partial \delta + \partial \epsilon + \partial \zeta + \partial \eta + \partial \theta + \partial i + \partial \kappa + \partial \lambda + \partial \mu + \\
& \partial v + \partial \xi + \partial o + \partial \pi + \partial \rho + \partial \sigma + \partial \tau + \partial v + \partial \phi + \partial \chi + \partial \psi + \partial \omega + \\
& \partial \varepsilon + \partial \vartheta + \partial \varpi + \partial \varrho + \partial \varsigma + \partial \varphi + \partial \ell + \partial \wp + \\
& \partial A + \partial B + \partial \Gamma + \partial \Delta + \partial E + \partial Z + \partial H + \partial \Theta + \partial I + \partial K + \partial \Lambda + \partial M + \\
& \partial N + \partial \Xi + \partial O + \partial \Pi + \partial P + \partial \Sigma + \partial T + \partial \Upsilon + \partial \Phi + \partial X + \partial \Psi + \partial \Omega +
\end{aligned}$$

## 2.7 Slash kerning

$1/A + 1/B + 1/C + 1/D + 1/E + 1/F + 1/G + 1/H + 1/I + 1/J + 1/K + 1/L + 1/M +$   
 $1/N + 1/O + 1/P + 1/Q + 1/R + 1/S + 1/T + 1/U + 1/V + 1/W + 1/X + 1/Y + 1/Z +$   
 $1/a + 1/b + 1/c + 1/d + 1/e + 1/f + 1/g + 1/h + 1/i + 1/j + 1/k + 1/l + 1/m +$   
 $1/n + 1/o + 1/p + 1/q + 1/r + 1/s + 1/t + 1/u + 1/v + 1/w + 1/x + 1/y + 1/z + 1/\iota + 1/\jmath +$   
 $1/A + 1/B + 1/\Gamma + 1/\Delta + 1/E + 1/Z + 1/H + 1/\Theta + 1/I + 1/K + 1/\Lambda + 1/M +$   
 $1/N + 1/\Xi + 1/O + 1/\Pi + 1/P + 1/\Sigma + 1/T + 1/\Upsilon + 1/\Phi + 1/X + 1/\Psi + 1/\Omega +$   
 $1/\alpha + 1/\beta + 1/\gamma + 1/\delta + 1/\epsilon + 1/\zeta + 1/\eta + 1/\theta + 1/\iota + 1/\kappa + 1/\lambda + 1/\mu +$   
 $1/v + 1/\xi + 1/o + 1/\pi + 1/\rho + 1/\sigma + 1/\tau + 1/v + 1/\phi + 1/\chi + 1/\psi + 1/\omega +$   
 $1/\varepsilon + 1/\vartheta + 1/\varpi + 1/\varrho + 1/\varsigma + 1/\varphi + 1/\ell + 1/\wp +$

$A/2 + B/2 + C/2 + D/2 + E/2 + F/2 + G/2 + H/2 + I/2 + J/2 + K/2 + L/2 + M/2 +$   
 $N/2 + O/2 + P/2 + Q/2 + R/2 + S/2 + T/2 + U/2 + V/2 + W/2 + X/2 + Y/2 + Z/2 +$   
 $a/2 + b/2 + c/2 + d/2 + e/2 + f/2 + g/2 + h/2 + i/2 + j/2 + k/2 + l/2 + m/2 +$   
 $n/2 + o/2 + p/2 + q/2 + r/2 + s/2 + t/2 + u/2 + v/2 + w/2 + x/2 + y/2 + z/2 + \iota/2 + \jmath/2 +$   
 $A/2 + B/2 + \Gamma/2 + \Delta/2 + E/2 + Z/2 + H/2 + \Theta/2 + I/2 + K/2 + \Lambda/2 + M/2 +$   
 $N/2 + \Xi/2 + O/2 + \Pi/2 + P/2 + \Sigma/2 + T/2 + \Upsilon/2 + \Phi/2 + X/2 + \Psi/2 + \Omega/2 +$   
 $\alpha/2 + \beta/2 + \gamma/2 + \delta/2 + \epsilon/2 + \zeta/2 + \eta/2 + \theta/2 + \iota/2 + \kappa/2 + \lambda/2 + \mu/2 +$   
 $v/2 + \xi/2 + o/2 + \pi/2 + \rho/2 + \sigma/2 + \tau/2 + v/2 + \phi/2 + \chi/2 + \psi/2 + \omega/2 +$   
 $\varepsilon/2 + \vartheta/2 + \varpi/2 + \varrho/2 + \varsigma/2 + \varphi/2 + \ell/2 + \wp/2 +$

## 2.8 Big operators

$$\begin{array}{c}
\sum_{i=1}^n x^n \quad \prod_{i=1}^n x^n \quad \coprod_{i=1}^n x^n \quad \int_{i=1}^n x^n \quad \oint_{i=1}^n x^n \\
\bigotimes_{i=1}^n x^n \quad \bigoplus_{i=1}^n x^n \quad \bigodot_{i=1}^n x^n \quad \bigwedge_{i=1}^n x^n \quad \bigvee_{i=1}^n x^n \quad \biguplus_{i=1}^n x^n \quad \bigcup_{i=1}^n x^n \quad \bigcap_{i=1}^n x^n \quad \bigsqcup_{i=1}^n x^n
\end{array}$$

## 2.9 Radicals

$$\begin{array}{c}
\sqrt{x+y} \quad \sqrt{x^2+y^2} \quad \sqrt{x_i^2+y_j^2} \quad \sqrt{\left(\frac{\cos x}{2}\right)} \quad \sqrt{\left(\frac{\sin x}{2}\right)} \\
\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{\sqrt{x+y}}}}}}
\end{array}$$

## 2.10 Over- and underbraces

$$\overbrace{x} \quad \overbrace{x+y} \quad \overbrace{x^2+y^2} \quad \overbrace{x_i^2+y_j^2} \quad \underbrace{x} \quad \underbrace{x+y} \quad \underbrace{x_i+y_j} \quad \underbrace{x_i^2+y_j^2}$$

## 2.11 Normal and wide accents

$$\dot{x} \quad \ddot{x} \quad \vec{x} \quad \bar{x} \quad \overline{xx} \quad \tilde{x} \quad \widetilde{x} \quad \widehat{xx} \quad \widehat{x} \quad \widehat{\widehat{x}} \quad \widehat{\widehat{\widehat{x}}}$$

## 2.12 Long arrows

$$\longleftrightarrow \quad \leftrightarrow \quad \leftarrow \quad \rightarrow \quad \longleftrightarrow \quad \Longleftrightarrow \quad \Leftrightarrow \quad \Leftarrow \quad \Rightarrow \quad \Longleftrightarrow$$

## 2.13 Left and right delimiters

$$-(f) -- [f] -- \lfloor f \rfloor -- \lceil f \rceil -- \langle f \rangle -- \{ f \} --$$

$$\begin{aligned}
& - (f) -- [f] -- \lfloor f \rfloor -- \lceil f \rceil -- \langle f \rangle -- \{ f \} -- \\
& - )f( -- ]f[ -- /f/ -- \backslash f \backslash -- /f \backslash -- \backslash f / --
\end{aligned}$$

## 2.14 Big-g-g delimiters

## 2.15 Symbols

This is from [2]

Symbol	Control Sequence	mathcode	Family	Hex Position
$\partial$	partial	"0140	1	40
$\flat$	flat	"015B	1	5B
$\natural$	natural	"015C	1	5C
$\sharp$	sharp	"015D	1	5D
$\ell$	ell	"0160	1	60
$\imath$	imath	"017B	1	7B
$\jmath$	jmath	"017C	1	7C
$\wp$	wp	"017D	1	7D
$'$	prime	"0230	2	30
$\infty$	infty	"0231	2	31
$\triangle$	triangle	"0234	2	34
$\forall$	forall	"0238	2	38
$\exists$	exists	"0239	2	39
$\neg$	neg	"023A	2	3A
$\emptyset$	emptyset	"023B	2	3B
$\Re$	Re	"023C	2	3C
$\Im$	Im	"023D	2	3D

⊤	top	"023E	2	3E
⊥	bot	"023F	2	3F
ℵ	aleph	"0240	2	40
∇	nabla	"0272	2	72
♣	clubsuit	"027C	2	7C
◊	diamondsuit	"027D	2	7D
♡	heartsuit	"027E	2	7E
♠	spadesuit	"027F	2	7F
∫ ∫	smallint	"1273	2	73
⊻ ⊻	bigsqcup	"1346	3	46
∮ ∮	ointop	"1348	3	48
⊕ ⊙	bigdot	"134A	3	4A
⊕ ⊕	bigoplus	"134C	3	4C
⊗ ⊗	bigotimes	"134E	3	4E
Σ Σ	sum	"1350	3	50
Π Π	prod	"1351	3	51
∫ ∫	intop	"1352	3	52
⊻ ⊻	bigcup	"1353	3	53
⊓ ⊓	bigcap	"1354	3	54
⊕ ⊕	biguplus	"1355	3	55
⊓ ⊓	bigwedge	"1356	3	56
⊓ ⊓	bigvee	"1357	3	57
⊻ ⊻	coprod	"1360	3	60
▷	triangleright	"212E	1	2E
◁	triangleleft	"212F	1	2F
★	star	"213F	1	3F
.	cldot	"2201	2	01
×	times	"2202	2	02
*	ast	"2203	2	03
÷	div	"2204	2	04
◊	diamond	"2205	2	05
±	pm	"2206	2	06
∐	mp	"2207	2	07
⊕	oplus	"2208	2	08
⊖	ominus	"2209	2	09
⊗	otimes	"220A	2	0A
⊘	oslash	"220B	2	0B
⊙	odot	"220C	2	0C
○	bigcirc	"220D	2	0D
◦	circ	"220E	2	0E

•	bullet	"220F	2	0F
△	bigtriangleup	"2234	2	34
▽	bigtriangledown	"2235	2	35
∪	cup	"225B	2	5B
∩	cap	"225C	2	5C
⊕	uplus	"225D	2	5D
∧	wedge	"225E	2	5E
∨	vee	"225F	2	5F
\	setminus	"226E	2	6E
↷	wr	"226F	2	6F
II	amalg	"2271	2	71
□	sqcup	"2274	2	74
□	sqcap	"2275	2	75
†	dagger	"2279	2	79
‡	ddagger	"227A	2	7A
↶	leftharpoonup	"3128	1	28
↷	leftharpoondown	"3129	1	29
↷	rightharpoonup	"312A	1	2A
↷	rightharpoondown	"312B	1	2B
↷	smile	"315E	1	5E
↷	frown	"315F	1	5F
↷	asymp	"3210	2	10
↷	equiv	"3211	2	11
↷	subseteq	"3212	2	12
↷	supseteq	"3213	2	13
↷	leq	"3214	2	14
↷	geq	"3215	2	15
↷	preceq	"3216	2	16
↷	succeq	"3217	2	17
↷	sim	"3218	2	18
↷	approx	"3219	2	19
↷	subset	"321A	2	1A
↷	supset	"321B	2	1B
↷	ll	"321C	2	1C
≪	gg	"321D	2	1D
≫	prec	"321E	2	1E
↷	succ	"321F	2	1F
←	leftarrow	"3220	2	20
→	rightarrow	"3221	2	21
↔	leftrightarrow	"3224	2	24
↗	nearrow	"3225	2	25
↘	searrow	"3226	2	26
↷	simeq	"3227	2	27
⇒	Leftarrow	"3228	2	28
⇒	Rightarrow	"3229	2	29
⇒	Leftrightarrow	"322C	2	2C

$\nwarrow$	nwarrown	"322D	2	2D
$\swarrow$	swarrow	"322E	2	2E
$\propto$	proto	"322F	2	2F
$\in$	in	"3232	2	32
$\ni$	ni	"3233	2	33
$/$	not	"3236	2	36
$\mapstochar$	mapstochar	"3237	2	37
$\perp$	perp	"323F	2	3F
$\vdash$	vdash	"3260	2	60
$\dashv$	dashv	"3261	2	61
$ $	mid	"326A	2	6A
$\parallel$	parallel	"326B	2	6B
$\sqsubseteq$	sqsubseteq	"3276	2	76
$\sqsupseteq$	sqsupseteq	"3277	2	77

## 2.16 Miscellaneous formulae

Taken from [3]

$$\hbar\nu = E, \quad \hbar \neq \pi, \quad \partial j, \quad x^j, \quad x^l$$

Some other other equations:  $\sum^J a'$ ,  $r^a$  and  $D^k$ .

Let  $\mathbf{A} = (a_{ij})$  be the adjacency matrix of graph  $G$ . The corresponding Kirchhoff matrix  $\mathbf{K} = (k_{ij})$  is obtained from  $\mathbf{A}$  by replacing in  $-\mathbf{A}$  each diagonal entry by the degree of its corresponding vertex; i.e., the  $i$ th diagonal entry is identified with the degree of the  $i$ th vertex. It is well known that

$$\det \mathbf{K}(i|i) = \text{the number of spanning trees of } G, \quad i = 1, \dots, n \quad (5)$$

where  $\mathbf{K}(i|i)$  is the  $i$ th principal submatrix of  $\mathbf{K}$ .

Let  $C_{i(j)}$  be the set of graphs obtained from  $G$  by attaching edge  $(v_i v_j)$  to each spanning tree of  $G$ . Denote by  $C_i = \bigcup_j C_{i(j)}$ . It is obvious that the collection of Hamiltonian cycles is a subset of  $C_i$ . Note that the cardinality of  $C_i$  is  $k_{ii} \det \mathbf{K}(i|i)$ . Let  $\hat{X} = \{\hat{x}_1, \dots, \hat{x}_n\}$ . Define multiplication for the elements of  $\hat{X}$  by

$$\hat{x}_i \hat{x}_j = \hat{x}_j \hat{x}_i, \quad \hat{x}_i^2 = 0, \quad i, j = 1, \dots, n. \quad (6)$$

Let  $\hat{k}_{ij} = k_{ij} \hat{x}_j$  and  $\hat{k}_{ij} = -\sum_{j \neq i} \hat{k}_{ij}$ . Then the number of Hamiltonian cycles  $H_c$  is given by the relation

$$\left( \prod_{j=1}^n \hat{x}_j \right) H_c = \frac{1}{2} \hat{k}_{ii} \det \widehat{\mathbf{K}}(i|i), \quad i = 1, \dots, n. \quad (7)$$

The task here is to express (7) in a form free of any  $\hat{x}_i$ ,  $i = 1, \dots, n$ . The result also leads to the resolution of enumeration of Hamiltonian paths in a graph.

It is well known that the enumeration of Hamiltonian cycles and paths in a complete graph  $K_n$  and in a complete bipartite graph  $K_{n_1 n_2}$  can only be found from

*first combinatorial principles.* One wonders if there exists a formula which can be used very efficiently to produce  $K_n$  and  $K_{n_1 n_2}$ . Recently, using Lagrangian methods, Goulden and Jackson have shown that  $H_c$  can be expressed in terms of the determinant and permanent of the adjacency matrix. However, the formula of Goulden and Jackson determines neither  $K_n$  nor  $K_{n_1 n_2}$  effectively. In this paper, using an algebraic method, we parametrize the adjacency matrix. The resulting formula also involves the determinant and permanent, but it can easily be applied to  $K_n$  and  $K_{n_1 n_2}$ . In addition, we eliminate the permanent from  $H_c$  and show that  $H_c$  can be represented by a determinantal function of multivariables, each variable with domain  $\{0, 1\}$ . Furthermore, we show that  $H_c$  can be written by number of spanning trees of subgraphs. Finally, we apply the formulas to a complete multigraph  $K_{n_1 \dots n_p}$ .

The conditions  $a_{ij} = a_{ji}$ ,  $i, j = 1, \dots, n$ , are not required in this paper. All formulas can be extended to a digraph simply by multiplying  $H_c$  by 2.

The boundedness, property of  $\Phi_0$ , then yields

$$\int_{\mathcal{D}} |\bar{\partial}u|^2 e^{\alpha|z|^2} \geq c_6 \alpha \int_{\mathcal{D}} |u|^2 e^{\alpha|z|^2} + c_7 \delta^{-2} \int_A |u|^2 e^{\alpha|z|^2}.$$

Let  $B(X)$  be the set of blocks of  $\Lambda_X$  and let  $b(X) = |B(X)|$ . If  $\phi \in Q_X$  then  $\phi$  is constant on the blocks of  $\Lambda_X$ .

$$P_X = \{\phi \in M \mid \Lambda_\phi = \Lambda_X\}, \quad Q_X = \{\phi \in M \mid \Lambda_\phi \geq \Lambda_X\}. \quad (8)$$

If  $\Lambda_\phi \geq \Lambda_X$  then  $\Lambda_\phi = \Lambda_Y$  for some  $Y \geq X$  so that

$$Q_X = \bigcup_{Y \geq X} P_Y.$$

Thus by Möbius inversion

$$|P_Y| = \sum_{X \geq Y} \mu(Y, X) |Q_X|.$$

Thus there is a bijection from  $Q_X$  to  $W^{B(X)}$ . In particular  $|Q_X| = w^{b(X)}$ .

$$W(\Phi) = \begin{vmatrix} \frac{\varphi}{(\varphi_1, \varepsilon_1)} & 0 & \dots & 0 \\ \frac{\varphi k_{n2}}{(\varphi_2, \varepsilon_1)} & \frac{\varphi}{(\varphi_2, \varepsilon_2)} & \dots & 0 \\ \dots & \dots & \dots & \dots \\ \frac{\varphi k_{n1}}{(\varphi_n, \varepsilon_1)} & \frac{\varphi k_{n2}}{(\varphi_n, \varepsilon_2)} & \dots & \frac{\varphi k_{nn-1}}{(\varphi_n, \varepsilon_{n-1})} & \frac{\varphi}{(\varphi_n, \varepsilon_n)} \end{vmatrix}$$

## References

- [1] Walter Schmidt. *Using Common PostScript Fonts With L<sup>A</sup>T<sub>E</sub>X. PSNFSS Version 9.2*, September 2004. <http://ctan.tug.org/tex-archive/macros/latex/required/psnfss>.
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- [3] Michael Downes and Barbara Beeton. *The amsart, amsproc, and amsbook document classes*. American Mathematical Society, August 2004. <http://www.ctan.org/tex-archive/macros/latex/required/amslatex/classes>.